



Spatial Computations and Rasters

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Math 241

Week 5 | Spring 2026



Week 5 Goals

Mon Lecture

- Introduction to spatial data
 - point data
 - polygon data
- Static and interactive maps with point and polygon data
 - base layers (almost as good as merino)
 - coordinate reference systems / projections
 - popups and additional context
 - static graphs with `sf` and `ggplot2`
 - interactive graphs with `leaflet`

Wed Lecture

- Geospatial computations
 - distance
 - spatial joins
- Raster data
 - what is it?
 - rasters as base layers
 - rasters as data
 - extracting values by polygons



Geospatial Computations



Geospatial Computations

Just like we can perform computations with numerical or factor data, we can compute new variables using spatial data

We'll look at a few helpful `sf` functions:

- `st_distance()`: compute distances between spatial objects
- `st_area()`: compute area enclosed by a spatial object
- `st_centroid()`: compute the centroid of a spatial object
- `st_length()`: compute the length of a spatial object
- `st_intersection()` and `st_difference()`: compute intersections or set differences of spatial objects
- `st_join()`: merge spatial data based on spatial relationships



New data: MacLeish Property

- liberal arts field station at Smith College
- 250 acre area of forest and pasture land near Whately, MA
- Smith College community can use the space for artistic inquiry, environmental research, outdoor education, low-impact recreation

Can read in spatial data from `macleish` package

```
1 library(macleish)
2 str(macleish_layers, max.level = 1)
```

List of 12

```
$ landmarks      :Classes 'sf' and 'data.frame': 14 obs. of  2 variables:
 ..- attr(*, "sf_column")= chr "geometry"
 ..- attr(*, "agr")= Factor w/ 3 levels "constant","aggregate",...: NA
 .. ..- attr(*, "names")= chr "Label"
$ forests        :Classes 'sf' and 'data.frame': 54 obs. of  5 variables:
 ..- attr(*, "sf_column")= chr "geometry"
 ..- attr(*, "agr")= Factor w/ 3 levels "constant","aggregate",...: NA NA NA NA
 .. ..- attr(*, "names")= chr [1:4] "VegType_20" "VegType_21" "Sheet1__Ve" "type"
$ streams        :Classes 'sf' and 'data.frame': 13 obs. of  2 variables:
 ..- attr(*, "sf_column")= chr "geometry"
 ..- attr(*, "agr")= Factor w/ 3 levels "constant","aggregate",...: NA
 .. ..- attr(*, "names")= chr "Id"
$ challenge_courses:Classes 'sf' and 'data.frame': 12 obs. of  24 variables:
```



MacLeish Property

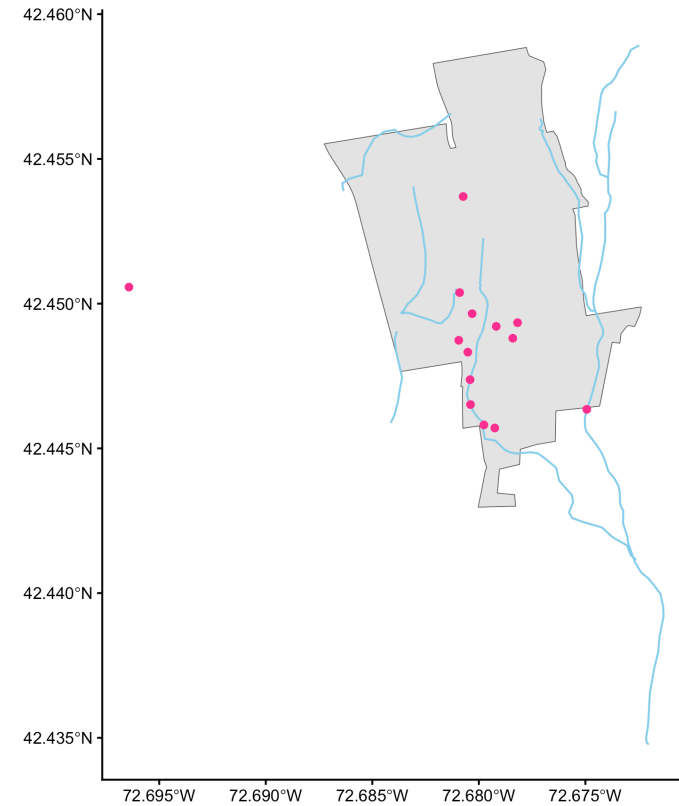
We'll start by taking a look at:

- The **landmarks** on the property (POINTS)
- The **boundary** of the property (POLYGON)
- The **streams** that go through the property (New geometry: LINESTRING)

```
1 landmarks <- macleish_layers$landmarks
2 boundary <- macleish_layers$boundary
3 streams <- macleish_layers$streams
```

MacLeish Property: Plotting

```
1 ggplot() +  
2   geom_sf(data = boundary) +  
3   geom_sf(data = streams, color = "skyblue") +  
4   geom_sf(data = landmarks, color = "deeppink") +  
5   theme_classic()
```



Distances: `st_distance()`

Can use the `st_distance()` function to compute the distance between two spatial objects:

```
1 library(sf)
2 # calculate distance between the first five landmarks
3 distance_matrix <- st_distance(landmarks[1:5, ])
4 distance_matrix
```

```
Units: [m]
      [,1]      [,2]      [,3]      [,4]      [,5]
[1,]  0.000 1328.4169 1333.0100 1824.4163 1390.4456
[2,] 1328.417  0.00000  598.0400  508.1877  201.6394
[3,] 1333.010  598.0400  0.00000  946.0184  799.6426
[4,] 1824.416  508.1877  946.0184  0.00000  448.1404
[5,] 1390.446  201.6394  799.6426  448.1404  0.00000
```

```
1 library(units)
2 distance_matrix %>%
3   set_units("mi") # distance in miles
```

```
Units: [mi]
      [,1]      [,2]      [,3]      [,4]      [,5]
[1,] 0.0000000 0.8254400 0.8282940 1.1336397 0.8639829
[2,] 0.8254400 0.0000000 0.3716048 0.3157732 0.1252929
[3,] 0.8282940 0.3716048 0.0000000 0.5878286 0.4968749
[4,] 1.1336397 0.3157732 0.5878286 0.0000000 0.2784615
[5,] 0.8639829 0.1252929 0.4968749 0.2784615 0.0000000
```

This distance is “**as the crow flies**”

- There are other options (e.g., distance by driving) – see Chapter 18 in MDSR!



Calculating area: `st_area()`

The `boundary` dataset already reports the area of the plot:

```
1 boundary$area
255.0989 [acre]
```

But we could calculate it ourselves with the `st_area()` function

```
1 st_area(boundary) %>%
2   set_units("acres")
255.0989 [acres]
```

Centroids: `st_centroid()`

Can calculate the centroid of the **boundary** using the `st_centroid()`

```
1 boundary_center <- st_centroid(boundary)
2 boundary_center
```

Simple feature collection with 1 feature and 1 field

Geometry type: POINT

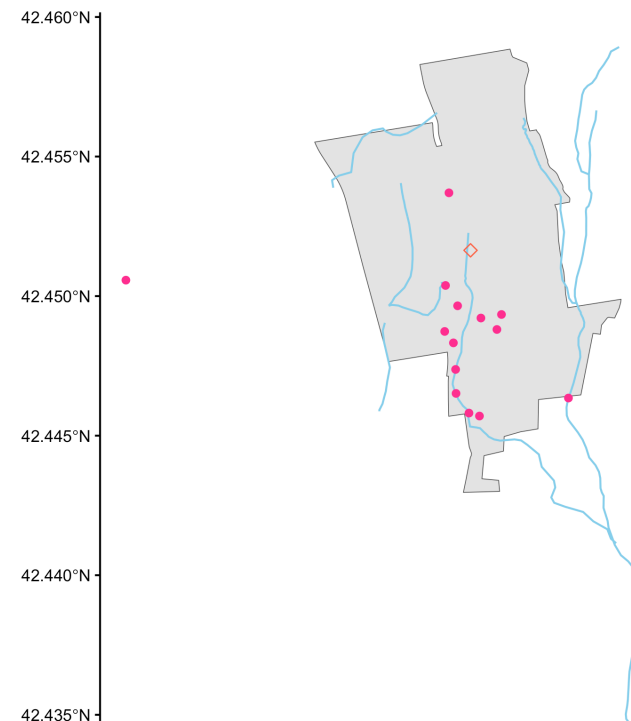
Dimension: XY

Bounding box: xmin: -72.67969 ymin: 42.45164 xmax: -72.67969 ymax: 42.45164

Geodetic CRS: WGS 84

```
      area      geometry
1 255.0989 [acre] POINT (-72.67969 42.45164)
```

```
1 ggplot() +
2   geom_sf(data = boundary) +
3   geom_sf(data = streams,
4           color = "skyblue") +
5   geom_sf(data = landmarks,
6           color = "deeppink") +
7   geom_sf(data = boundary_center,
8           shape = 5, size = 2,
9           color = "tomato") +
10  labs(caption = "Red diamond indicates boundary center")
11  theme_classic()
```



Lengths of lines/edges: `st_length()`

Can compute the length of each stream with the `st_length()` function (from `sf`)

```
1 streams <- streams %>%
2   mutate(length = st_length(geometry))
3 streams
```

Simple feature collection with 13 features and 2 fields

Geometry type: LINESTRING

Dimension: XY

Bounding box: xmin: -72.68641 ymin: 42.43476 xmax: -72.67133 ymax: 42.45892

Geodetic CRS: WGS 84

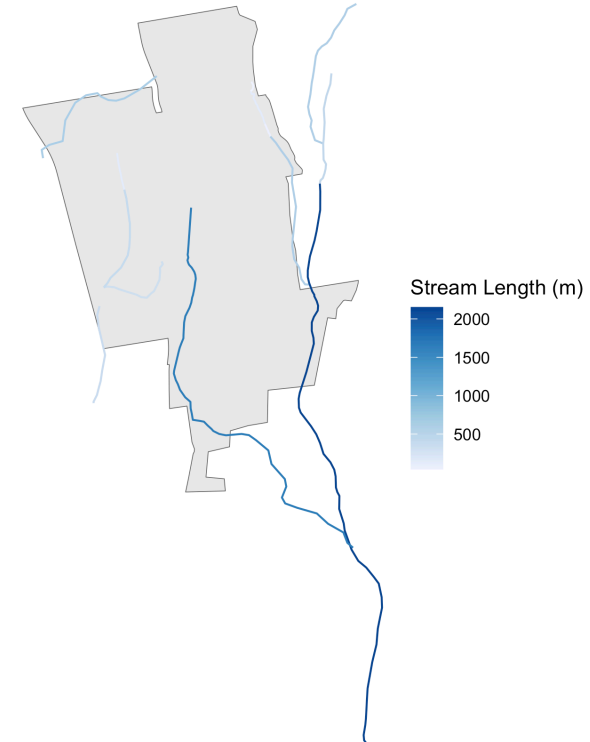
First 10 features:

	Id	geometry	length
1	1	LINESTRING (-72.67247 42.45...	593.33436 [m]
2	1	LINESTRING (-72.67357 42.45...	412.27916 [m]
3	1	LINESTRING (-72.67652 42.45...	137.87960 [m]
4	1	LINESTRING (-72.67715 42.45...	40.25734 [m]
5	1	LINESTRING (-72.67652 42.45...	51.02365 [m]
6	1	LINESTRING (-72.67628 42.45...	592.79892 [m]
7	1	LINESTRING (-72.67409 42.45...	2152.43892 [m]

Lengths of lines/edges: `st_length()`

Coloring streams by length:

```
1 ggplot(boundary) +  
2   geom_sf() +  
3   geom_sf(data = streams, aes(color = as.numeric(length  
4     scale_color_distiller(palette = "Blues", direction =  
5     labs(color = "Stream Length (m)")) +  
6   theme_void()
```



Intersections: `st_intersection()` and `st_difference()`

`st_intersection()` can retain only the parts of the streams that lie *within* the boundary:

```
1 streams_within <- st_intersection(streams, boundary)
2 streams_within
```

Simple feature collection with 11 features and 3 fields

Geometry type: GEOMETRY

Dimension: XY

Bounding box: xmin: -72.68622 ymin: 42.44482 xmax: -72.67416 ymax: 42.45657

Geodetic CRS: WGS 84

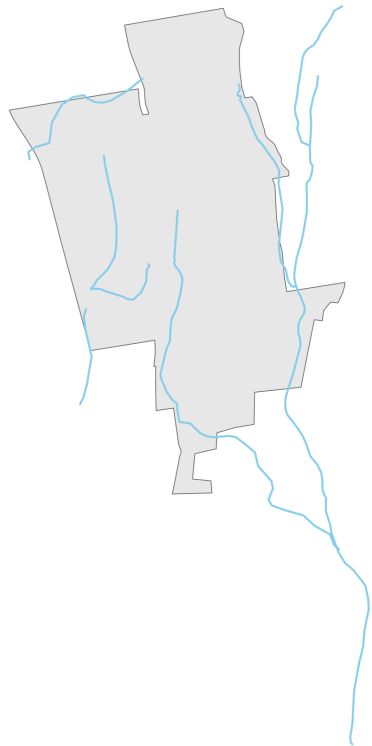
First 10 features:

	Id	length	area	geometry
3	1	137.87960 [m]	255.0989 [acre]	LINestring (-72.67652 42.45...
4	1	40.25734 [m]	255.0989 [acre]	LINestring (-72.67715 42.45...
5	1	51.02365 [m]	255.0989 [acre]	LINestring (-72.67652 42.45...
6	1	592.79892 [m]	255.0989 [acre]	MULTILINestring ((-72.67628...
7	1	2152.43892 [m]	255.0989 [acre]	LINestring (-72.67448 42.44...
8	3	1651.25471 [m]	255.0989 [acre]	LINestring (-72.67979 42.45...
9	3	316.21854 [m]	255.0989 [acre]	LINestring (-72.68109 42.45...

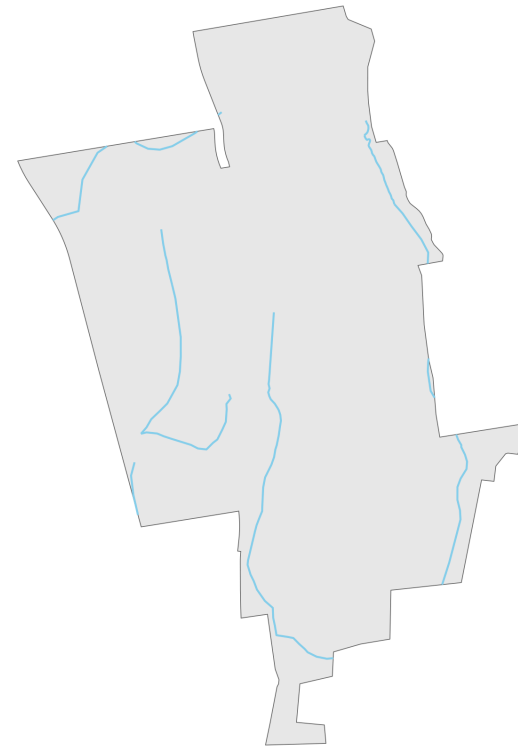
- Note that the intersection returns the **lines** from **streams** not the polygon from **boundary**.

Intersections: `st_intersection()` and `st_difference()`

```
1 ggplot(boundary) +  
2   geom_sf() +  
3   geom_sf(data = streams, color = "skyblue") +  
4   theme_void()
```



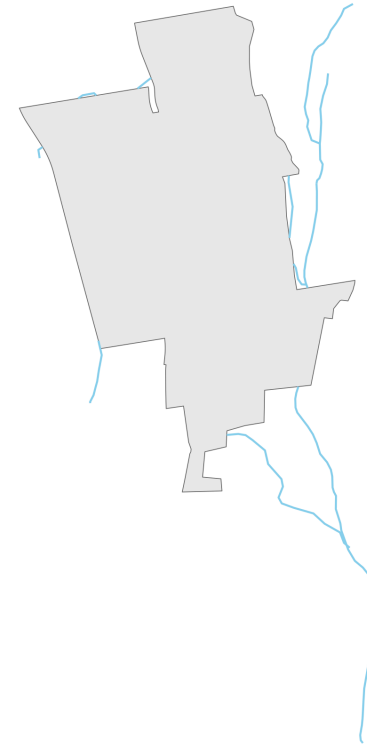
```
1 ggplot(boundary) +  
2   geom_sf() +  
3   geom_sf(data = streams_within, color = "skyblue") +  
4   theme_void()
```



Intersections: `st_intersection()` and `st_difference()`

`st_difference()` can retain only the parts of the streams that lie *outside* the boundary:

```
1 streams_outside <- st_difference(streams, boundary)
2 ggplot(boundary) +
3   geom_sf() +
4   geom_sf(data = streams_outside, color = "skyblue") +
5   theme_void()
```



Intersections: `st_intersection()` and `st_difference()`

Another example: Let's pull out the trails in this station

```
1 trails <- macleish_layers$trails
2 trails
```

Simple feature collection with 15 features and 2 fields

Geometry type: LINESTRING

Dimension: XY

Bounding box: xmin: -72.68513 ymin: 42.44177 xmax: -72.67731 ymax: 42.4618

Geodetic CRS: WGS 84

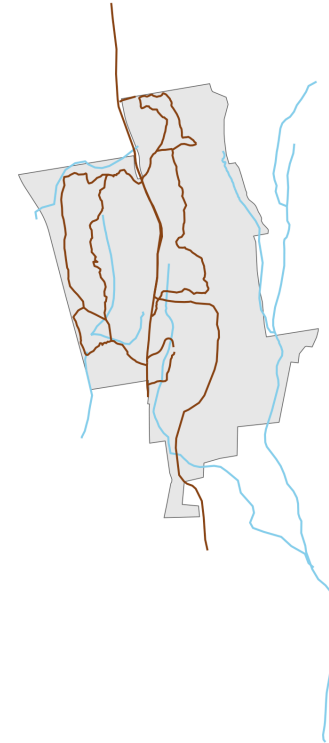
First 10 features:

	name	color	geometry
1	Porcupine Trail	White	LINESTRING (-72.68291 42.45...
2	Western Loop	Red	LINESTRING (-72.68111 42.45...
3	Poplar Hill Road	Road	LINESTRING (-72.68155 42.45...
4	Vernal Pool Loop	Yellow	LINESTRING (-72.68265 42.44...
5	Eastern Loop	Blue	LINESTRING (-72.68113 42.45...
6	Western Loop	Red	LINESTRING (-72.68401 42.45...
7	Western Loop	Red	LINESTRING (-72.68088 42.44...



Intersections: `st_intersection()` and `st_difference()`

```
1 ggplot(boundary) +  
2   geom_sf() +  
3   geom_sf(data = streams, color = "skyblue") +  
4   geom_sf(data = trails, color = "chocolate4") +  
5   theme_void()
```



Intersections: `st_intersection()` and `st_difference()`

...and see where they intersect with the streams!

```
1 intersections <- st_intersection(trails, streams)
2 intersections
```

Simple feature collection with 10 features and 4 fields

Geometry type: GEOMETRY

Dimension: XY

Bounding box: xmin: -72.68389 ymin: 42.44529 xmax: -72.67941 ymax: 42.45644

Geodetic CRS: WGS 84

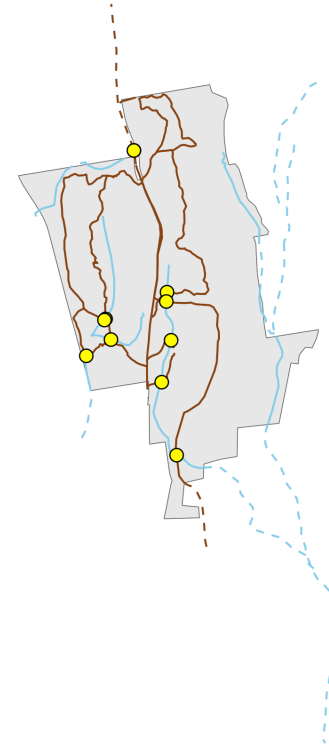
	name	color	Id	length	geometry
8	entry trail	-	3	1651.2547 [m]	POINT (-72.68015 42.44796)
9	Eastern Loop	Blue	3	1651.2547 [m]	POINT (-72.67989 42.45126)
13	Snowmobile Trail	<NA>	3	1651.2547 [m]	MULTIPOINT ((-72.67992 42.4...
15	Driveway	<NA>	3	1651.2547 [m]	POINT (-72.67968 42.4495)
6	Western Loop	Red	3	316.2185 [m]	POINT (-72.68267 42.44952)
1	Porcupine Trail	White	3	388.2598 [m]	POINT (-72.68293 42.45028)
6.1	Western Loop	Red	3	388.2598 [m]	POINT (-72.68299 42.45024)
4	Vernal Pool Loop	Yellow	3	362.6555 [m]	POINT (-72.68389 42.44893)

- Note that **the intersection geometries are now *points***



Intersections: `st_intersection()` and `st_difference()`

```
1 trails_within <- st_intersection(trails, boundary)
2 trails_outside <- st_difference(trails, boundary)
3
4 ggplot(boundary) +
5   geom_sf() +
6   geom_sf(data = streams_within,
7           color = "skyblue") +
8   geom_sf(data = streams_outside,
9           color = "skyblue",
10          linetype = "dashed") +
11  geom_sf(data = trails_within,
12          color = "chocolate4") +
13  geom_sf(data = trails_outside,
14          color = "chocolate4",
15          linetype = "dashed") +
16  geom_sf(data = intersections,
17          shape = 21,
18          fill = "yellow").
```



- Plotted stream crossing!

Aggregation

Let's look at the trails data frame a little more:

```
1 trails %>%  
2   arrange(name)
```

Simple feature collection with 15 features and 2 fields

Geometry type: LINESTRING

Dimension: XY

Bounding box: xmin: -72.68513 ymin: 42.44177 xmax: -72.67731 ymax: 42.4618

Geodetic CRS: WGS 84

First 10 features:

	name	color	geometry
1	Driveway	<NA>	LINESTRING (-72.68088 42.44...
2	Eastern Loop	Blue	LINESTRING (-72.68113 42.45...
3	Eastern Loop	Blue	LINESTRING (-72.68063 42.45...
4	Easy Out	Red	LINESTRING (-72.67962 42.45...
5	Easy Out	<NA>	LINESTRING (-72.68144 42.45...
6	Poplar Hill Road	Road	LINESTRING (-72.68155 42.45...
7	Poplar Hill Road	Road	LINESTRING (-72.68087 42.44...

What is odd about this data frame?



Aggregation

Let's look at the "Eastern Loop"

```
1 eastern <- trails %>% filter(name=="Eastern Loop")
2 eastern
```

Simple feature collection with 2 features and 2 fields

Geometry type: LINESTRING

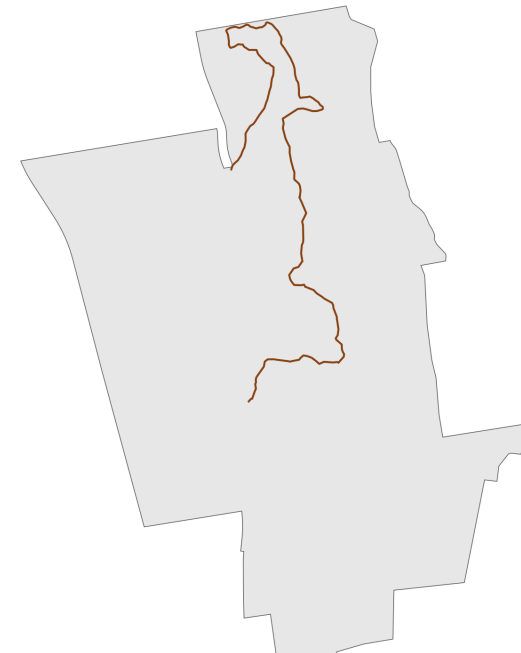
Dimension: XY

Bounding box: xmin: -72.68127 ymin: 42.45033 xmax: -72.67783 ymax: 42.4585

Geodetic CRS: WGS 84

	name	color	geometry
1	Eastern Loop	Blue	LINESTRING (-72.68113 42.45...
2	Eastern Loop	Blue	LINESTRING (-72.68063 42.45...

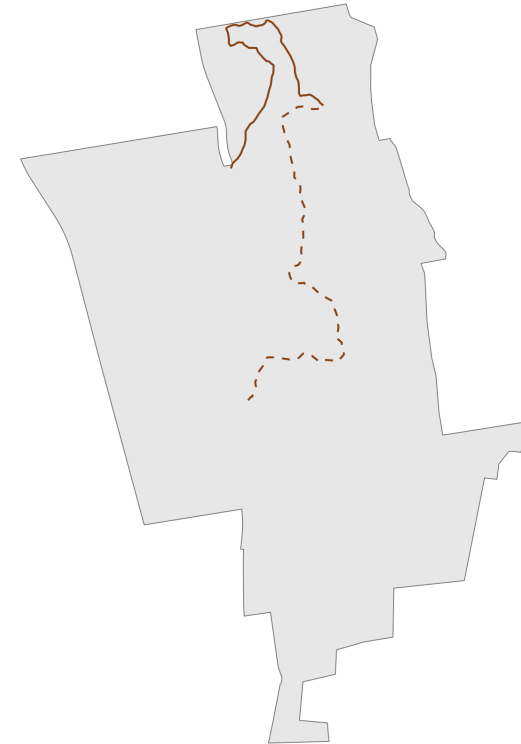
```
1 ggplot(boundary) +
2   geom_sf() +
3   geom_sf(data = eastern, color = "chocolate4") +
4   theme_void()
```



Aggregation

What are the pieces of this trail?

```
1 part_one <- eastern[1, ]
2 part_two <- eastern[2, ]
3 ggplot(boundary) +
4   geom_sf() +
5   geom_sf(data = part_one,
6           color = "chocolate4") + # part 1
7   geom_sf(data = part_two,
8           color = "chocolate4",
9           linetype = "dashed") + # part 2
10  theme_void()
```



Aggregation

For plotting this is fine, but what if we wanted to compare the lengths of each trail?

```
1 trails %>%  
2   mutate(trail_length = st_length(geometry)) %>%  
3   arrange(desc(trail_length))
```

Simple feature collection with 15 features and 3 fields

Geometry type: LINESTRING

Dimension: XY

Bounding box: xmin: -72.68513 ymin: 42.44177 xmax: -72.67731 ymax: 42.4618

Geodetic CRS: WGS 84

First 10 features:

	name	color	trail_length	geometry
1	Snowmobile Trail	<NA>	1346.9147 [m]	LINESTRING (-72.68053 42.45...
2	Snowmobile Trail	<NA>	1229.1787 [m]	LINESTRING (-72.68053 42.45...
3	Eastern Loop	Blue	1107.9588 [m]	LINESTRING (-72.68063 42.45...
4	Western Loop	Red	969.0932 [m]	LINESTRING (-72.68111 42.45...
5	Poplar Hill Road	Road	900.5781 [m]	LINESTRING (-72.68155 42.45...
6	Eastern Loop	Blue	831.2864 [m]	LINESTRING (-72.68113 42.45...
7	Porcupine Trail	White	699.7393 [m]	LINESTRING (-72.68291 42.45...

The same trail comes up multiple times! How can we combine them?

- `group_by()` and `summarize()`



Aggregation: `group_by` and `summarize()`

```
1 trails_combined <- trails %>%
2   group_by(name) %>%
3   summarize(trail_length = sum(st_length(geometry))) %>%
4   arrange(desc(trail_length))
5 trails_combined
```

Simple feature collection with 9 features and 2 fields

Geometry type: GEOMETRY

Dimension: XY

Bounding box: xmin: -72.68513 ymin: 42.44177 xmax: -72.67731 ymax: 42.4618

Geodetic CRS: WGS 84

A tibble: 9 × 3

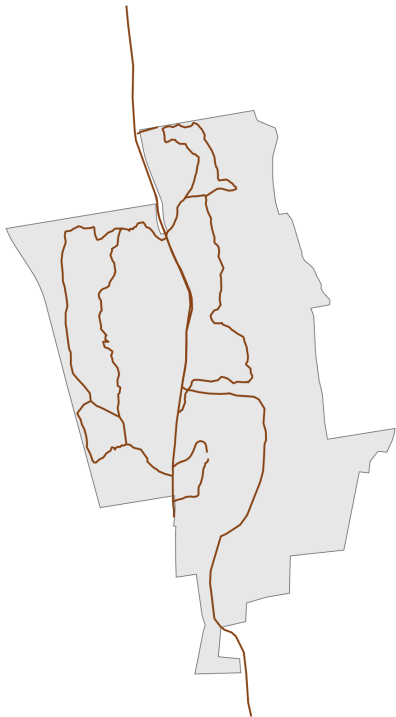
name <chr>	trail_length [m]	geometry <GEOMETRY [°]>
1 Snowmobile Trail	2576.	MULTILINESTRING ((-72.68053 42.45106, -72.68035...
2 Eastern Loop	1939.	MULTILINESTRING ((-72.68113 42.45531, -72.68111...
3 Western Loop	1350.	MULTILINESTRING ((-72.68111 42.45526, -72.68129...
4 Poplar Hill Road	1040.	MULTILINESTRING ((-72.68155 42.45649, -72.68149...
5 Porcupine Trail	700.	LINestring (-72.68291 42.45021, -72.68296 42.45...
6 Vernal Pool Loop	360.	LINestring (-72.68265 42.44944, -72.68274 42.44...

Only one row now for each trail.



Aggregation: `group_by` and `summarize()`

```
1 # Not combining
2 ggplot(boundary) +
3   geom_sf() +
4   geom_sf(data = trails,
5           color = "chocolate4") +
6   theme_void()
```



```
1 # Combined
2 ggplot(boundary) +
3   geom_sf() +
4   geom_sf(data = trails_combined,
5           color = "chocolate4") +
6   theme_void()
```

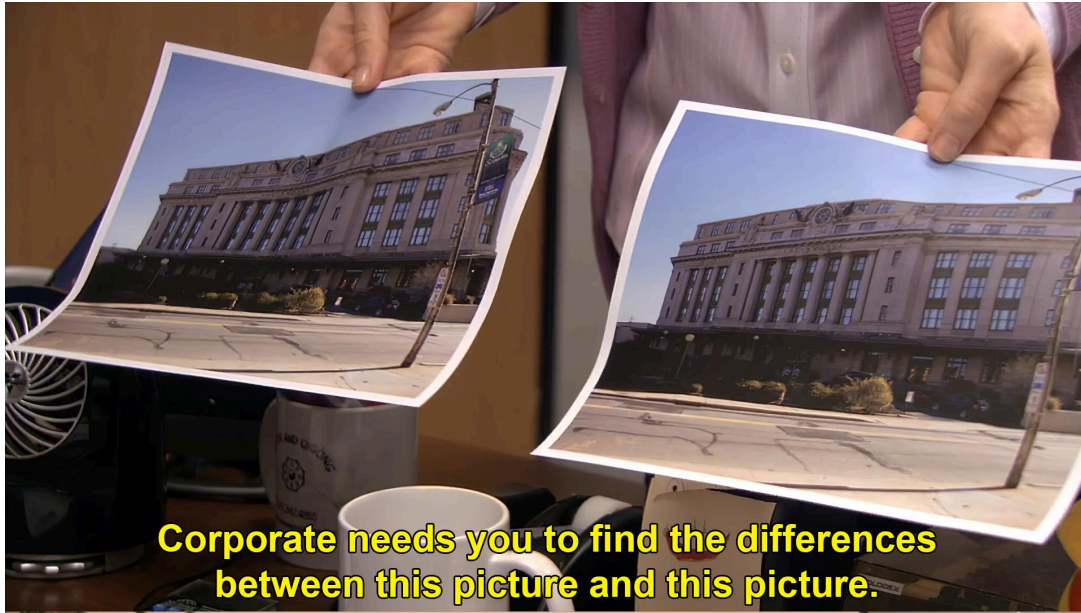


01:00



Find the difference in the plots!!

Aggregation: `group_by` and `summarize()`



Merging Spatial data: `st_join()`

```
1 forests <- macleish_layers$forests %>%
2   select(type, geometry)
3 camp_sites <- macleish_layers$camp_sites %>%
4   select(name, geometry)
```

1 forests

Simple feature collection with 54 features and 1 field

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: -72.68726 ymin: 42.44292 xmax:
-72.67237 ymax: 42.45884

Geodetic CRS: WGS 84

First 10 features:

	type
geometry	
1	<NA> MULTIPOLYGON (((-72.68079
4...	
2	Abandoned Pasture MULTIPOLYGON (((-72.67814
4...	
3	Active Pasture and Hayfield MULTIPOLYGON (((-72.67974
.	

1 camp_sites

Simple feature collection with 2 features and 1 field

Geometry type: POINT

Dimension: XY

Bounding box: xmin: -72.67958 ymin: 42.45098 xmax:
-72.67815 ymax: 42.45855

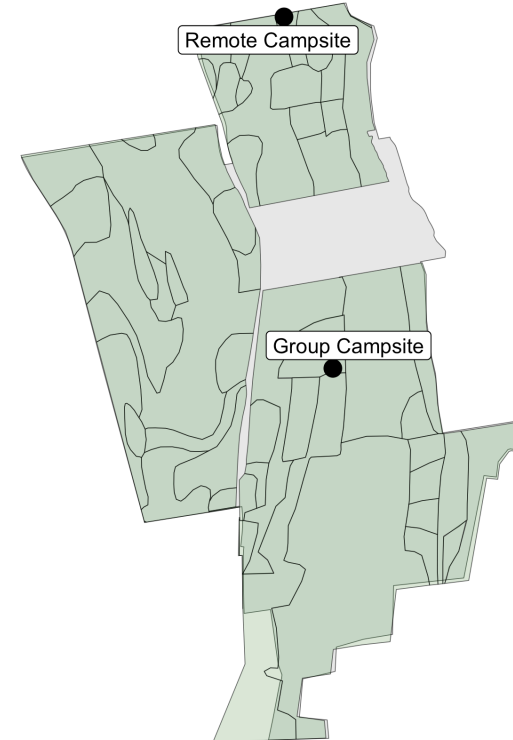
Geodetic CRS: WGS 84

A tibble: 2 × 2

name	geometry
<chr>	<POINT [°]>
1 Group Campsite	(-72.67815 42.45098)
2 Remote Campsite	(-72.67958 42.45855)

Merging Spatial data: `st_join()`

```
1 library(ggspatial)
2 ggplot(boundary) +
3   geom_sf() +
4   geom_sf(data = forests, fill = "forestgreen",
5           alpha = 0.2) +
6   geom_sf(data = camp_sites, size = 4) +
7   geom_sf_label_repel(data = camp_sites,
8                       aes(label = name)) +
9   theme_void()
```



What if we wanted to know **which forests** these campsites are in?

Merging Spatial data: `st_join()`

`st_join()` can merge datasets on spatial data.

```
1 camp_sites_forests <- st_join(camp_sites, forests, left = TRUE)
2 camp_sites_forests
```

Simple feature collection with 2 features and 2 fields

Geometry type: POINT

Dimension: XY

Bounding box: xmin: -72.67958 ymin: 42.45098 xmax: -72.67815 ymax: 42.45855

Geodetic CRS: WGS 84

A tibble: 2 × 3

	name	geometry	type
*	<chr>	<POINT [°]>	<chr>
1	Group Campsite	(-72.67815 42.45098)	Old Field White Pine Forest
2	Remote Campsite	(-72.67958 42.45855)	Sugar Maple Forest

- Setting `left = TRUE` yields a `left_join()` here. `left = FALSE` would yield an `inner_join()`.

You can set the `join` argument to specify *how* you want to connect the geometries.

- `join = st_intersects` is the default, but other `st_*` functions can be specified.



Raster data

What are raster data?

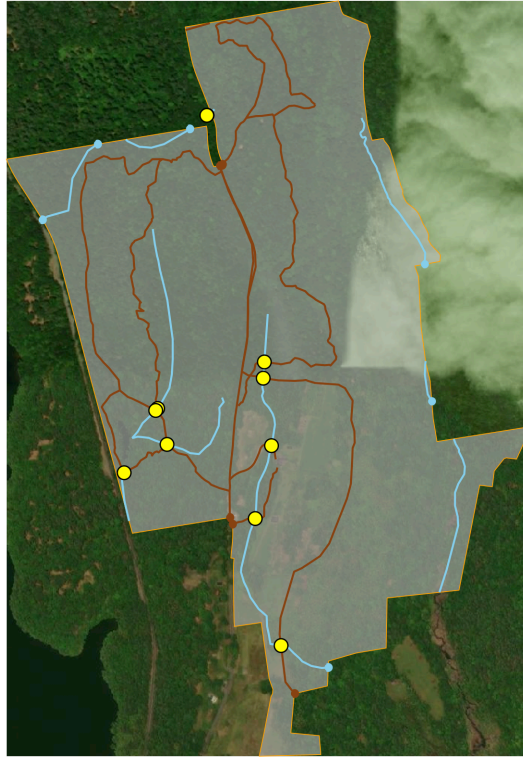
- So far, we've dealt with (multi)points, (multi)polygons, and line(string) data!
 - These all fall into the family of “vector” spatial data
 - Called “vectors” since they are made up of discrete x, y coordinates that compose a shape.
- Now, we are entering into the world of **raster** spatial data.
- Raster data are arrays of spatially indexed cells, each of the same size
- Think: **spatially indexed matrix** or **image**. Each cell / pixel..
 - is a predefined size square
 - is the same size as the other cells / pixels
 - has value(s) attached to it

Raster data: two hats

- We'll use raster data in two distinct ways:
 - as a **base layer** for maps, and
 - as **data** for maps.

Raster as base layer: example

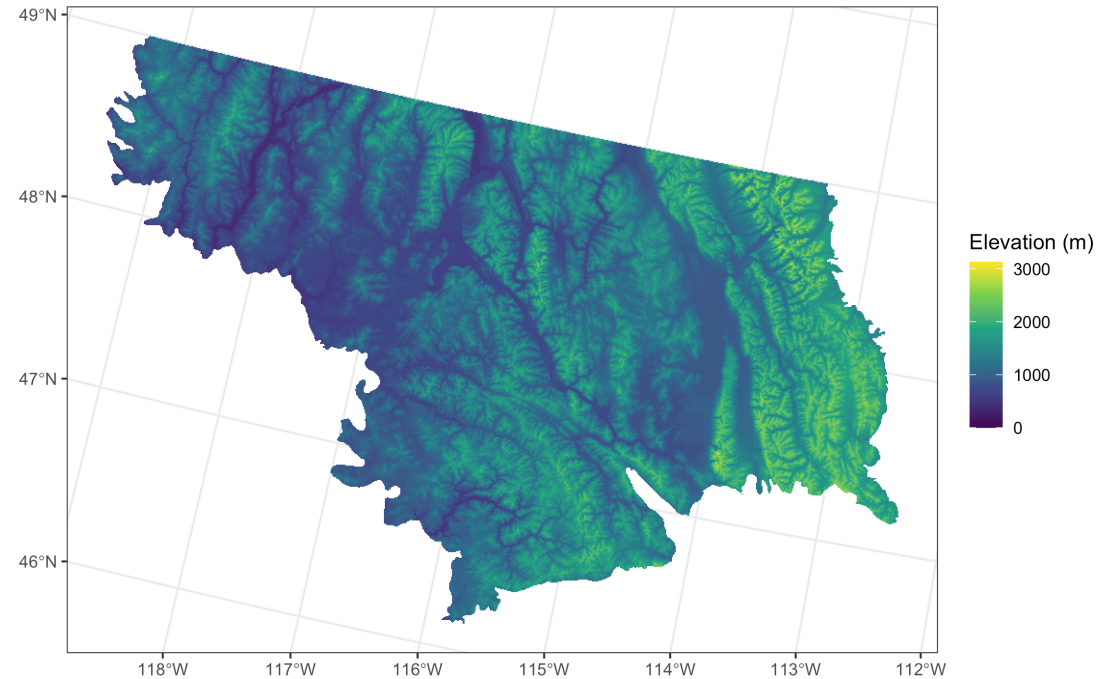
2.39m x 2.39m imagery in the Macleish property



- Each pixel is a 2.39m x 2.39m square and has RED, GREEN, BLUE (RGB) values assigned to it.

Raster as data: example

90m x 90m elevation data in M333 “ecoprovince” (NE Washington, N Idaho, W Montana)



- Each pixel is a 90m x 90m square and has an elevation value assigned to it.

Loading raster data



We'll use the `terra` R package to deal with rasters.

- `terra` can also handle many vector data types such as points and polygons.
 - But `sf` is often nicer to work with for those data types.
- Raster data are often stored as Geotiff (.tif) files.

```
1 library(terra)
2 r <- terra::rast("data/M333_elev.tif")
3 class(r)
```

```
[1] "SpatRaster"
attr(,"package")
[1] "terra"
```

```
1 r
```

```
class      : SpatRaster
size       : 4083, 5509, 1 (nrow, ncol, nlyr)
resolution : 90, 90 (x, y)
extent     : -1736295, -1240485, 2731305, 3098775 (xmin, xmax, ymin, ymax)
coord. ref.: NAD_1983_Albers
source     : M333_elev.tif
name       : M333_elev
```

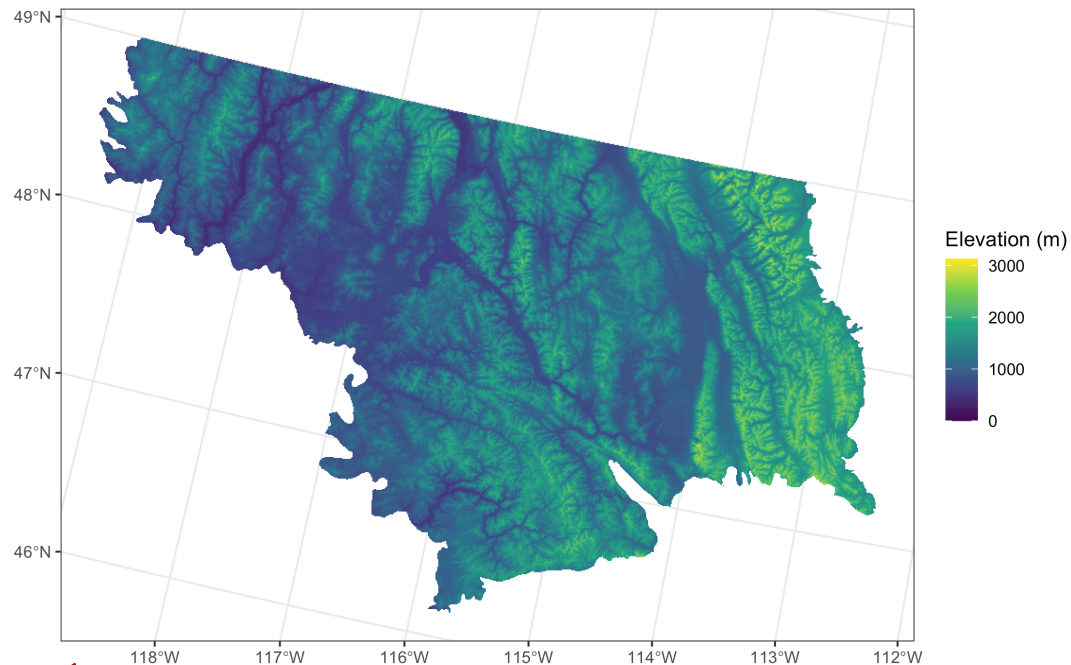


Plotting raster data

The `tidyterra` package gives us some nice `geom_*()` functions to use with `SpatRasters` and `SpatVectors`.

```
1 library(tidyterra)
2 ggplot() +
3   geom_spatraster(data = r, na.rm = TRUE) +
4   scale_fill_viridis_c(na.value = NA) +
5   labs(fill = "Elevation (m)") +
6   theme_bw()
```

- Main functions:
 - `geom_spatraster()` for rasters as data
 - `geom_spatraster_rgb()` for rasters as baselayers



Raster attributes

Rasters have CRSs as well!

```
1 crs(r)
```

```
[1] "PROJCRS[\"NAD_1983_Albers\", \n      BASEGEOGCRS[\"NAD83\", \n                  DATUM[\"North American Datum 1983\", \n                        ELLIPSOID[\"GRS 1980\", 6378137, 298.257222101004, \n                                  LENGTHUNIT[\"metre\", 1]], \n                        PRIMEM[\"Greenwich\", 0, \n                                ANGLEUNIT[\"degree\", 0.0174532925199433]], \n                        ID[\"EPSG\", 4269]], \n                  CONVERSION[\"Albers Equal Area\", \n                              METHOD[\"Albers Equal Area\", \n                                      ID[\"EPSG\", 9822]], \n                              PARAMETER[\"Latitude of false origin\", 23, \n                                          ANGLEUNIT[\"degree\", 0.0174532925199433], \n                                          ID[\"EPSG\", 8821]], \n                              PARAMETER[\"Longitude of false origin\", -96, \n                                          ANGLEUNIT[\"degree\", 0.0174532925199433], \n                                          ID[\"EPSG\", 8822]], \n                              PARAMETER[\"Latitude of 1st standard\n                              parallel\", 29.5, \n                                          ANGLEUNIT[\"degree\", 0.0174532925199433], \n                                          ID[\"EPSG\", 8823]], \n                              PARAMETER[\"Latitude of 2nd standard parallel\", 45.5, \n                                          ANGLEUNIT[\"degree\", 0.0174532925199433], \n                                          ID[\"EPSG\", 8824]], \n                              PARAMETER[\"Easting at false origin\", 0, \n                                          LENGTHUNIT[\"metre\", 1], \n                                          ID[\"EPSG\", 8826]], \n                              PARAMETER[\"Northing at false origin\", 0, \n                                          LENGTHUNIT[\"metre\", 1], \n                                          ID[\"EPSG\", 8827]]], \n      CS[Cartesian, 2], \n      AXIS[\"easting\", east, \n           ORDER[1], \n           LENGTHUNIT[\"metre\", 1], \n           ID[\"EPSG\", 9001]], \n      AXIS[\"northing\", north, \n           ORDER[2], \n           LENGTHUNIT[\"metre\", 1], \n           ID[\"EPSG\", 9001]]]"
```

And we can get summary stats from rasters

```
1 max(values(r), na.rm = TRUE) # highest elevation in M333
```

```
[1] 3188
```

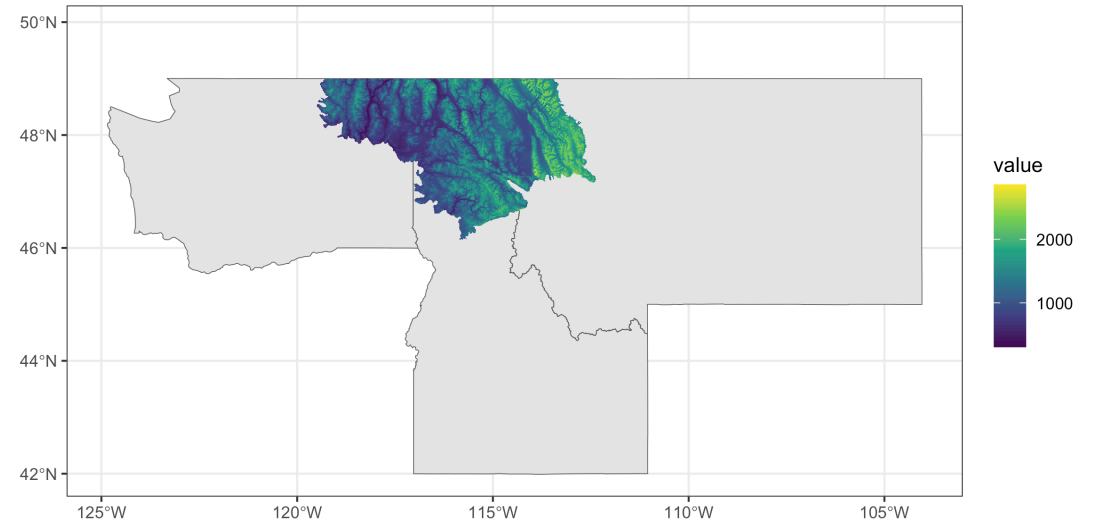
```
1 mean(values(r), na.rm = TRUE) # average elevation in M333
```

```
[1] 1256.759
```



Plotting rasters with vector data

```
1 library(tigris)
2 states(progress_bar = FALSE) %>%
3   filter(NAME %in% c("Washington",
4                     "Idaho",
5                     "Montana")) %>%
6   ggplot() +
7   geom_sf() +
8   geom_spatraster(data = r) +
9   scale_fill_viridis_c(na.value = NA) +
10  theme_bw()
```



- Since both the raster and polygons are spatially referenced they “play nice” together!

Extracting values from vectors that intersect our raster

- Sometimes, we'd like to know the value of a raster at a specific location
 - Think: elevation at a given point, or
 - average elevation in a national forest, etc.
- **terra** makes this easy.
- Let's get the elevation of the FIA plots in the **forested** package that intersect with our raster!

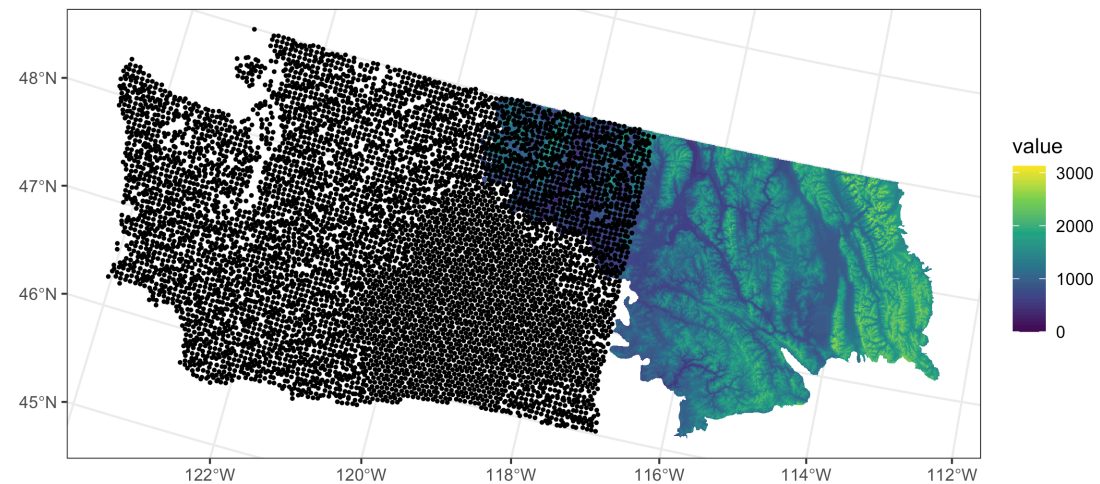
```
1 library(forested)
2 forested_sf <- forested %>%
3   st_as_sf(coords = c("lon", "lat"),
4             crs = "EPSG:4269")
5
6 plot_elev <- terra::extract(r, forested_sf, xy = TRUE)
7 plot_elev
```

	ID	M333_elev	x	y
1	1	881	-1672800	3055350
2	2	NA	NaN	NaN
3	3	NA	NaN	NaN
4	4	NA	NaN	NaN
5	5	806	-1630320	2974890
6	6	736	-1615560	2984610
7	7	636	-1575240	2986500
8	8	NA	NaN	NaN
9	9	NA	NaN	NaN
10	10	NA	NaN	NaN
11	11	NA	NaN	NaN
12	12	NA	NaN	NaN
13	13	NA	NaN	NaN

• Why so many NAs?

Not all plots intersect our raster!

```
1 ggplot() +  
2   geom_spatraster(data = r) +  
3   geom_sf(data = forested_sf, size = 0.5) +  
4   scale_fill_viridis_c(na.value = NA) +  
5   theme_bw()
```

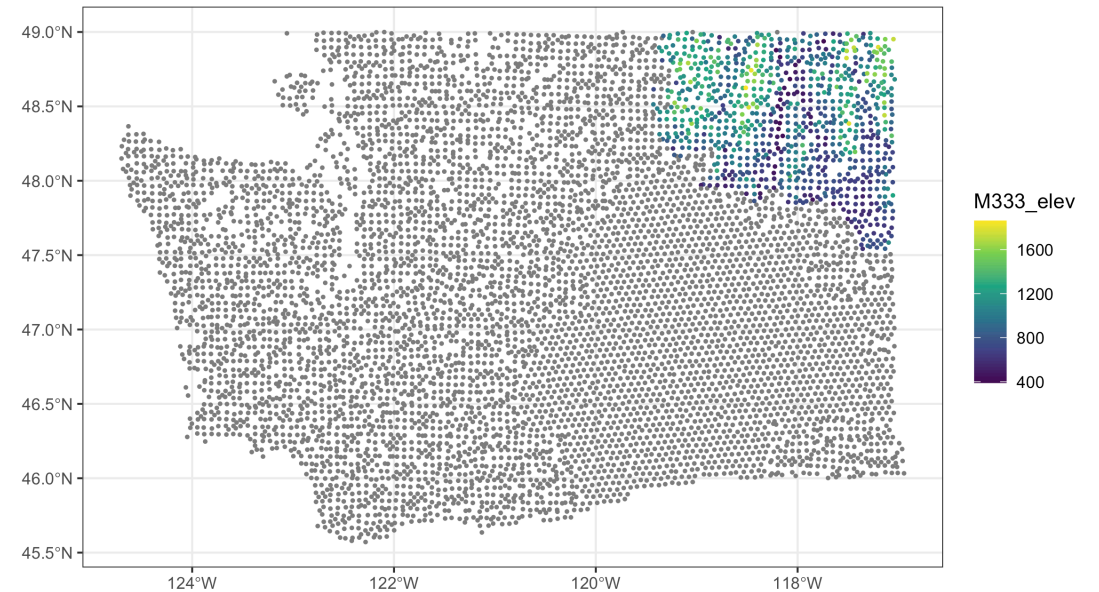


Bringing elevation values into the forested data

```
1 forested_with_M333_elev <- forested_sf %>%  
2   bind_cols(plot_elev)
```

- `bind_cols()` takes two data frames of the same number of rows and “pushes them together”.

```
1 forested_with_M333_elev %>%  
2   ggplot() +  
3   geom_sf(aes(color = M333_elev), size = 0.5) +  
4   scale_color_viridis_c() +  
5   theme_bw()
```



Elevation actually already exists in the **forested** dataset

```
1 mean(forested_with_M333_elev$elevation == forested_with_M333_elev$M333_elev)
```

```
[1] NA
```

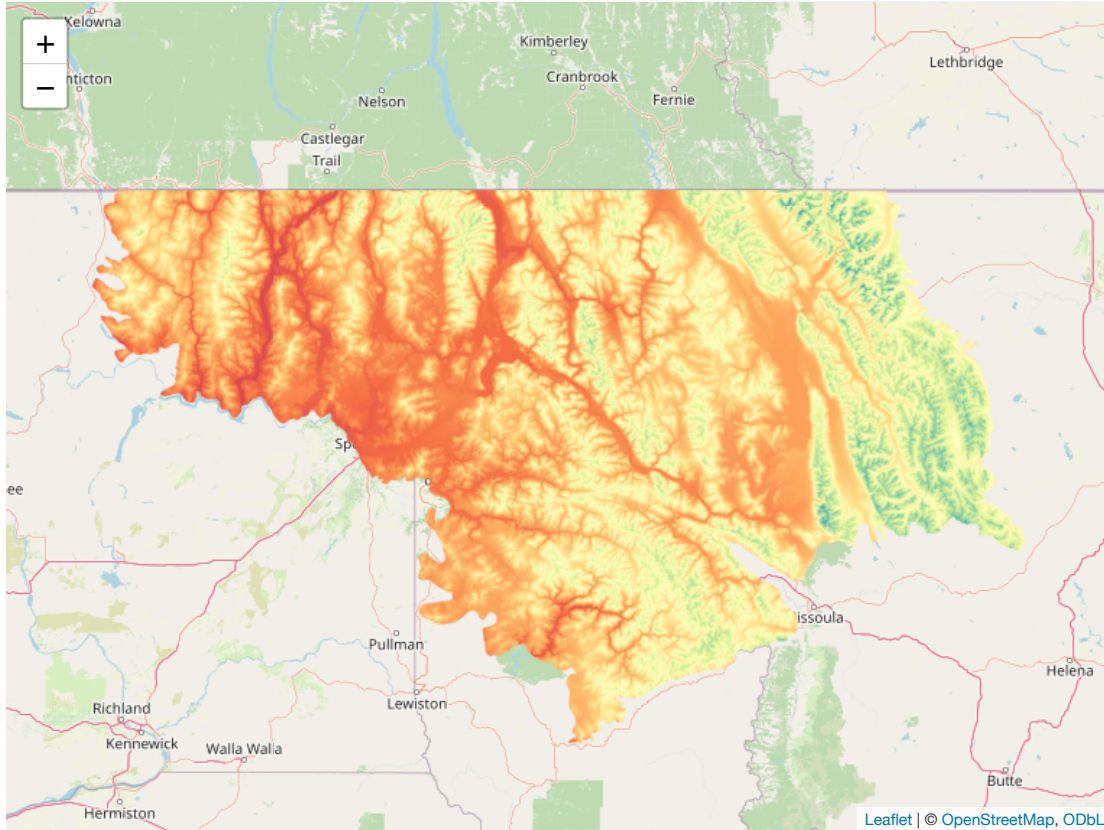
```
1 mean(forested_with_M333_elev$elevation == forested_with_M333_elev$M333_elev,  
2      na.rm = TRUE)
```

```
[1] 1
```

- When the data are available, we get the same result as the package!

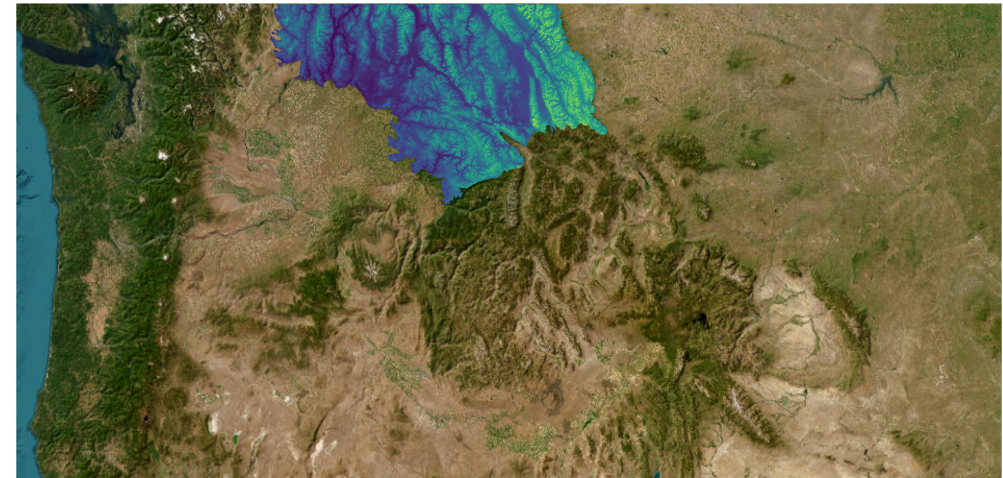
Interactive raster plots

```
1 library(leaflet)
2 leaflet() %>%
3   addTiles() %>%
4   addRasterImage(r, maxBytes = 15000000)
```



Plotting rasters with raster base layers

```
1 library(basemaps) # to get the raster base layers
2
3 wa_id_mt <- tigris::states(progress_bar = FALSE) %>%
4   filter(NAME %in% c("Washington",
5                     "Idaho",
6                     "Montana"))
7
8 rast <- basemap_terra(ext = wa_id_mt,
9                      map_service = "esri",
10                     map_type = "world_imagery",
11                     verbose = FALSE)
12
13 ggplot() +
14   geom_spatraster_rgb(data = rast) +
15   geom_spatraster(data = r) +
16   scale_fill_viridis_c(na.value = NA) +
17   labs(fill = "Elevation (m)") +
18   theme_void() +
```



Elevation (m)
1000 2000

- Using rasters in two ways: base layer and as data!

Returning to the Macleish Property

We can use a raster base layer and put vector data on top of it!

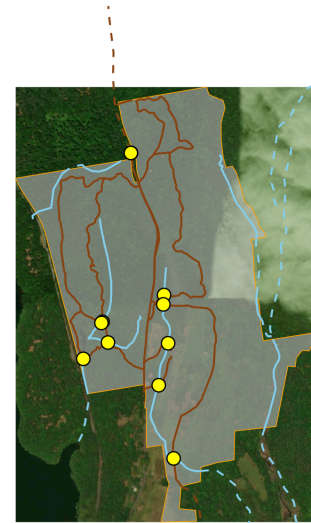
```
1 rast <- basemap_terra(  
2   # recall, `boundary` is the boundary  
3   # of the Macleish property  
4   ext = boundary,  
5   map_service = "esri",  
6   map_type = "world_imagery",  
7   verbose = FALSE  
8 )  
9  
10 ggplot() +  
11   geom_spatraster_rgb(data = rast) +  
12   geom_sf(data = boundary,  
13           alpha = 0.5,  
14           fill = "grey",  
15           color = "orange")
```



Returning to the Macleish Property

We can use a raster base layer and put vector data on top of it!

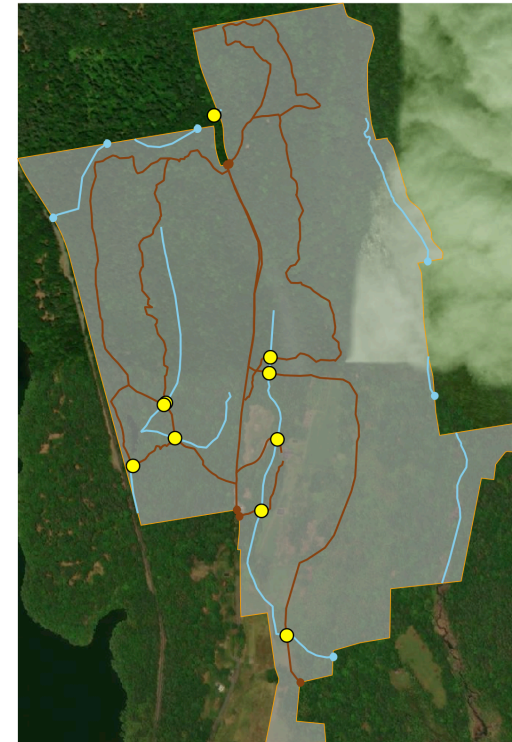
```
1 ggplot() +  
2   geom_spatraster_rgb(data = rast) +  
3   geom_sf(data = boundary,  
4           alpha = 0.5,  
5           fill = "grey",  
6           color = "orange") +  
7   geom_sf(data = streams_within,  
8           color = "skyblue") +  
9   geom_sf(data = streams_outside,  
10          color = "skyblue",  
11          linetype = "dashed") +  
12  geom_sf(data = trails_within,  
13          color = "chocolate4") +  
14  geom_sf(data = trails_outside ,  
15          color = "chocolate4",  
16          linetype = "dashed") +  
17  geom_sf(data = intersections,  
18          shape = 21.
```



Returning to the Macleish Property

We can use a raster base layer and put vector data on top of it!

```
1 ggplot() +  
2   geom_spatraster_rgb(data = rast) +  
3   geom_sf(data = boundary,  
4           alpha = 0.5,  
5           fill = "grey",  
6           color = "orange") +  
7   geom_sf(data = streams_within,  
8           color = "skyblue") +  
9   geom_sf(data = streams_outside %>%  
10          st_intersection(boundary),  
11          color = "skyblue",  
12          linetype = "dashed") +  
13  geom_sf(data = trails_within,  
14          color = "chocolate4") +  
15  geom_sf(data = trails_outside %>%  
16          st_intersection(boundary),  
17          color = "chocolate4",  
18          linetype = "dashed") +
```



- Note the use of `st_intersection()`

Spatial data: just scratching the surface

- We could spend all semester on spatial data...
- There is so much more we can do with rasters
 - raster algebra (adding / multiplying / etc. rasters)
 - reprojecting rasters to different resolutions
- You'll have opportunities in your projects to use spatial data if you'd like to!
- And lots of practice in Problem Set 4!



Next week

- Learn how to create interactive dashboards with **shiny**! (a great way to disseminate all of these interactive plots we've learned about)
- Get Project 1 instructions

